

# CBCS Scheme

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15MATDIP31

## Third Semester B.E. Degree Examination, Dec.2016/Jan.2017 Additional Mathematics – I

Time: 3 hrs.

Max. Marks: 80

*Note: Answer FIVE full questions, choosing one full question from each module.*

### Module-1

- 1 a. Simplify  $\frac{(\cos 3\theta - i \sin 3\theta)^2 (\cos 4\theta + i \sin 4\theta)^5}{(\cos \theta + i \sin \theta)^3 (\cos 2\theta - i \sin 2\theta)^4}$ . (06 Marks)
- b. Determine  $\lambda$  such that  $\vec{a} = \hat{i} + \hat{j} + \hat{k}$ ,  $\vec{b} = 2\hat{i} - 4\hat{k}$  and  $\vec{c} = \hat{i} + \lambda\hat{j} + 3\hat{k}$  are coplanar. (05 Marks)
- c. Find sine angle of two vectors  $4\hat{i} + 3\hat{j} + \hat{k}$  and  $2\hat{i} - \hat{j} + 2\hat{k}$ . (05 Marks)

OR

- 2 a. Express  $\frac{1}{2+i} - \frac{(1+i)^2}{3+i}$  in the form  $a + ib$ . (06 Marks)
- b. Find modulus and amplitude of  $1 + \cos \theta + i \sin \theta$ . (05 Marks)
- c. If  $\vec{a} = 3\hat{i} + 7\hat{j} - 2\hat{k}$ ,  $\vec{b} = 2\hat{i} + 5\hat{j} + 10\hat{k}$  find  $(\vec{a} + \vec{b}) \times (\vec{a} - \vec{b})$ . (05 Marks)

### Module-2

- 3 a. If  $y = a \cos(\log x) + b \sin(\log x)$  show that  $x^2 y_{n+2} + (2n+1)xy_{n+1} + (n^2+1)y_n = 0$ . (06 Marks)
- b. With usual notation prove that  $\tan \phi = r \frac{d\theta}{dr}$ . (05 Marks)
- c. If  $u = e^{ax+by} f(ax-by)$  prove that  $b \frac{\partial u}{\partial x} + a \frac{\partial u}{\partial y} = 2abu$ . (05 Marks)

OR

- 4 a. Find  $n^{\text{th}}$  derivative of  $y = e^x \sin 4x \cos x$  (06 Marks)
- b. Find pedal equation of  $r = a(1 + \cos \theta)$ . (05 Marks)
- c. If  $u = f(x-y, y-z, z-x)$  show that  $\frac{\partial u}{\partial x} + \frac{\partial u}{\partial y} + \frac{\partial u}{\partial z} = 0$ . (05 Marks)

### Module-3

- 5 a. Evaluate  $\int_0^{\pi} \sin^5(x/2) dx$ . (06 Marks)
- b. Evaluate  $\int_0^{2a} x^2 \sqrt{2ax - x^2} dx$ . (05 Marks)
- c. Evaluate  $\int_0^1 \int_x^{\sqrt{x}} xy dy dx$ . (05 Marks)

Important Note : 1. On completing your answers, compulsorily draw diagonal cross lines on the remaining blank pages.  
2. Any writing on the remaining blank pages will be treated as unfair means and will be penalized accordingly.

OR

- 6 a. Evaluate  $\int_0^a \frac{x^3 dx}{\sqrt{a^2 - x^2}}$ . (06 Marks)
- b. Evaluate  $\int_0^1 \int_0^{\sqrt{1-y^2}} x^3 dx dy$ . (05 Marks)
- c. Evaluate  $\int_0^a \int_0^x \int_0^{x+y} e^{x+y+z} dz dy dx$ . (05 Marks)

**Module-4**

- 7 a. A particle moves along the curve  $c : x = t^3 - 4t, y = t^2 + 4t, z = 8t^2 - 3t^3$  where  $t$  denotes time. Find velocity and acceleration at  $t = 2$ . (06 Marks)
- b. Find unit normal vector to surface  $Q = x^2yz + 4xz^2$  at  $(1, -2, -1)$ . (05 Marks)
- c. Show that  $\vec{f} = (2xy^2 + yz)\hat{i} + (2x^2y + xz + 2yz^2)\hat{j} + (2y^2z + xy)\hat{k}$  is irrotational. (05 Marks)

OR

- 8 a. A particle moves along the curve  $c : x = 2t^2, y = t^2 - 4t, z = 3t - 5$  where ' $t$ ' is the time. Find the components of velocity and acceleration at  $t = 1$  in the direction  $\hat{i} - 3\hat{j} + 2\hat{k}$ . (06 Marks)
- b. Find the angle between the surfaces  $x^2 + y^2 + z^2 = 9$  and  $z = x^2 + y^2 - 3$  at  $(2, -1, 2)$ . (05 Marks)
- c. If  $\phi = 2x^3y^2z^4$  find  $\text{div}(\text{grad}\phi)$ . (05 Marks)

**Module-5**

- 9 a. Solve :  $\sec^2x \tan y dx + \sec^2y \tan x dy = 0$ . (06 Marks)
- b. Solve :  $x^2y dx - (x^3 + y^3) dy = 0$ . (05 Marks)
- c. Solve :  $(y^3 - 3x^2y) dx - (x^3 - 3xy^2) dy = 0$ . (05 Marks)

OR

- 10 a. Solve :  $\frac{dy}{dx} = \frac{y}{x} + \sin\left(\frac{y}{x}\right)$ . (06 Marks)
- b. Solve :  $(x^2 + y^2 + x)dx + xy dy = 0$ . (05 Marks)
- c. Solve :  $\frac{dy}{dx} + y \cot x = \cos x$ . (05 Marks)

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